

# 1 **Influence of Alkali-Silica Reaction (ASR) on Aggregate Interlock in Reinforced Concrete**

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## 14 ABSTRACT:

15 Alkali-silica reaction (ASR) is one of the most damaging mechanisms affecting concrete structures  
16 worldwide. ASR effects on the durability and serviceability of damaged concrete are widely  
17 known and fairly well understood. However, the structural implications are still unclear, and a  
18 number of contradictory data are found in the literature, especially regarding shear behavior. The  
19 influence of ASR distressed reinforced concrete on aggregate interlock is presented in this paper.  
20 Push-off specimens having different reinforcement ratios were fabricated with ASR reactive  
21 coarse aggregates. The specimens were monitored over time and displayed different levels of  
22 expansion. Results indicated that ASR-induced expansion and damage were affected by the  
23 reinforcement ratio. However, little to no aggregate interlock reduction was observed on ASR-  
24 affected specimens up to moderate expansion levels. It was found that there were two controlling  
25 and competing mechanisms that affected aggregate interlock for ASR-affected specimens: the  
26 beneficial effects of chemical prestressing and the detrimental ASR-induced damage.

27 *Key words: Aggregate interlock, Alkali-Silica Reaction (ASR), Shear behavior, Push-off test,*  
28 *Expansion.*

## 29 1 INTRODUCTION

30 Alkali-silica reaction (ASR) is known as one of the most deleterious damage mechanisms for  
31 concrete. ASR is a chemical reaction between the alkali hydroxides from the concrete pore solution  
32 and some reactive siliceous phases from the aggregates [1-3]. ASR generates a product, the so

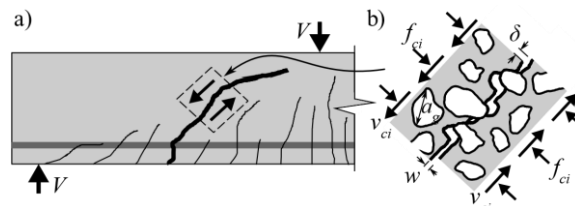
33 called alkali-silica gel, that swells in the presence of water, causing cracking and distress, which  
34 directly influences the concrete mechanical properties, especially the tensile strength and modulus  
35 of elasticity [1-3]. ASR effects on the durability and serviceability of affected concrete is widely  
36 known, while the structural implications on the long-term behavior is still unclear and a number  
37 of contradictory data are found in the literature, especially regarding the shear behavior of  
38 reinforced concrete elements affected by ASR.

### 39 1.1 Influence of ASR on the mechanical properties of affected concrete

40 Previous investigations have demonstrated that ASR has different effects on the mechanical  
41 properties of concrete such as the compressive strength, the tensile strength and the modulus of  
42 elasticity [4, 5]. Severe reduction in the tensile strength and the modulus of elasticity have been  
43 reported in literature while the compressive strength loss is typically less [4, 6]. These losses of  
44 tensile strength and modulus of elasticity at lower expansion levels seem to be linked to the  
45 formation of cracks within the aggregate particles. For higher levels of expansion, progression and  
46 interconnection of cracks within the cement paste seem to result in significant losses in the concrete  
47 compressive strength as well [1].

### 48 1.2 Influence of ASR on the structural behavior of affected structural members

49 Aspects of behavior of ASR affected structural elements that need further studies include:  
50 influence of cracking, loss of tensile and compressive strengths, loss of stiffness, influence of  
51 confinement effects (i.e., reinforcement ratio, external restraint), bond deterioration, aggregate  
52 interlock and the shear strength. It is well known that aggregate interlock has a strong influence  
53 on the shear strength (Figure 1). The concrete contribution to shear strength is due to both the  
54 tensile stresses in the diagonally cracked concrete and the aggregate interlock at the diagonal  
55 cracks [7-11]. This paper aims to understand the influence of ASR on aggregate interlock.



56

57 Figure 1: (a) Diagonal crack due to shear in reinforced concrete member and (b) close up of  
58 aggregate interlock at a crack

59 1.3 Aggregate interlock in reinforced concrete

60 Typically, push-off specimens with embedded stirrups (Figure 2a) are used to investigate  
61 aggregate interlock since the shear stress carry by this mechanism can be easily related to the crack  
62 width,  $w$ , and slip,  $\delta$ , and the normal pressure at the crack interface,  $f_{ci}$ . By subtracting the  
63 dowel action of the stirrups from the total shear,  $V$ , the shear stress due to aggregate interlock,  $v_{ci}$   
64 , can be determined as follows:

$$65 \quad v_{ci} = \frac{V}{A_c} - \rho v_d \quad (1)$$

66 Where  $v_d$  is the shear stress in the reinforcement,  $A_c$  is the shear plane area and  $\rho$  is the  
67 reinforcement ratio. The normal pressure at the crack interface,  $f_{ci}$ , can be determined from the  
68 stirrups axial stress,  $f_s$ , as follows:

$$69 \quad f_{ci} = \rho f_s \quad (2)$$

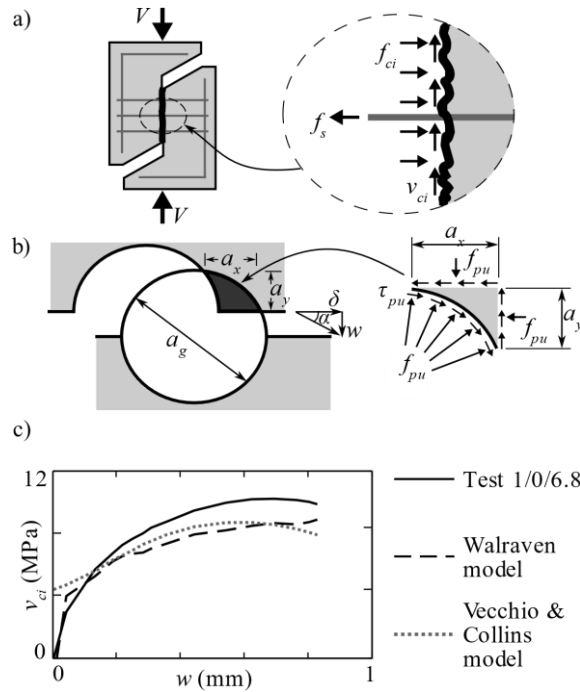
70 Walraven [12] carried out a large number of push-off tests (Figure 2a) and proposed an aggregate  
71 interlock model (Figure 2b). As illustrated in Figure 1b, aggregate interlock mechanism comes  
72 from the micro-roughened contact between the aggregate particles and the cement paste. The  
73 opening,  $w$ , and sliding,  $\delta$ , of a crack causes bearing of aggregates with the surrounding cement  
74 paste (Figure 2b). This bearing results in a shear stress,  $v_{ci}$ , and a normal stress,  $f_{ci}$ , acting  
75 perpendicularly to the crack plane. Thus, this aggregate interlock mechanism is directly related to  
76 the size, shape, amount and mechanical characteristics (i.e., stiffness, strength, hardness) of the  
77 coarse aggregate and cement paste as well as the amount of reinforcement crossing the crack.  
78 Increasing the crack width,  $w$ , or reducing the aggregates size,  $a_g$ , reduces the contact area  
79 between the aggregates and cement paste, which reduces the aggregate interlock. Increasing the  
80 concrete compressive strength enhances the bearing capacity of the aggregate-cement paste  
81 interface, which improves the aggregate interlock. However, the use of high-strength concrete  
82 (compressive strength measured on cylinder,  $f'_c$ , larger than 60 MPa) or concrete with weak  
83 aggregates can significantly reduce aggregate interlock because aggregate particles may fracture  
84 under stress at the crack [13-16].

85 By assuming a rigid-plastic stress-strain relationship between the aggregates and the surrounding  
 86 material matrix, the following equations were proposed to determine the aggregate interlock shear  
 87 stress,  $v_{ci}$ , and the resulting perpendicular stress,  $f_{ci}$  in normal strength concrete [12, 17].

$$88 \quad v_{ci} = -0.04f'_c + \left[ 1.8w^{-0.80} + (0.292w^{-0.707} - 0.25) f'_c \right] \delta \quad (3)$$

$$89 \quad f_{ci} = -0.06f'_c + \left[ 1.35w^{-0.63} + (0.242w^{-0.552} - 0.19) f'_c \right] \delta \quad (4)$$

90 These equations provide a relationship between the stress  $v_{ci}$  and  $f_{ci}$ , and the displacement at  
 91 crack  $w$  and  $\delta$ . This aggregate interlock model was validated by Walraven [12] as illustrated for  
 92 the test specimen 1/0/6.8 in Figure 2c. When aggregates particles are expected to fracture under  
 93 stress at cracks, that is for high-strength concrete or concrete with weak aggregates, Walraven et  
 94 al. [13] and fib [17] recommends reducing  $v_{ci}$  and  $f_{ci}$  determined from Eq. (3) and (4) by 65%.



95  
 96 Figure 2: (a) Push-off test to investigate aggregate interlock, (b) Walraven aggregate interlock  
 97 model and (c) comparison between analytical models and push-off test 1/0/6.8 carried out by  
 98 Walraven [12]

99 Vecchio et al. [18] proposed a simplified model to determine aggregate interlock capacity based  
 100 on the experiments carried out by Walraven [12]. This simplified model given by Eq. (5) can be

101 used to determine the interface shear stress at a crack due to aggregate interlock,  $v_{ci}$ , according to  
 102 the compressive stress across the crack interface,  $f_{ci}$ , and a maximum aggregate interlock shear  
 103 capacity,  $v_{ci,max}$ . This maximum aggregate interlock shear capacity given by Eq. (6) considers that  
 104 a larger crack width reduces the contact area and the aggregate interlock capacity while the use of  
 105 larger aggregates increases the contact area and the aggregate interlock capacity (see Figure 2).  
 106 For high-strength concrete or concrete containing weak aggregates, the aggregates may fracture  
 107 under stress and an aggregate size of 0 mm is suggested in Eq. (6) [19].

$$108 \quad v_{ci} = 0.18v_{ci,max} + 1.64f_{ci} - 0.82 \frac{f_{ci}^2}{v_{ci,max}} \quad (5)$$

$$109 \quad v_{ci,max} = \frac{\sqrt{f'_c}}{0.31 + 24w / (16 + a_g)} \quad (6)$$

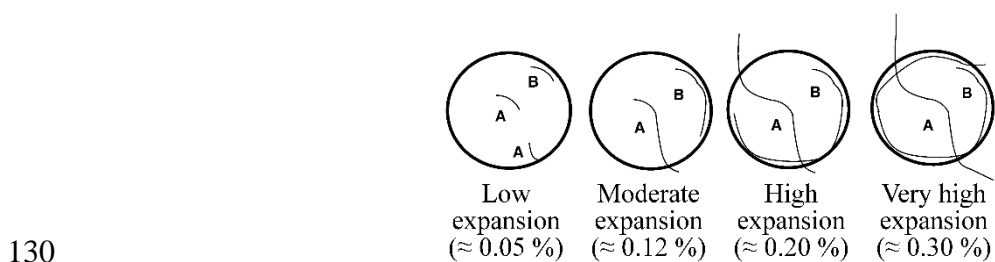
110 Figure 2c compares the prediction of one of Walraven's test specimens using Eq. (5). This  
 111 simplified model provides a good prediction of the aggregate interlock shear stress as a function  
 112 of the crack width. Due to its simplicity and accuracy, design codes are based on the model  
 113 developed by Vecchio and Collins to determine the interface shear capacity due to aggregate  
 114 interlock in reinforced concrete members [17, 20-22].

#### 115 1.4 ASR effects on concrete properties

116 The behavior of aggregate interlock in ASR-affected concrete is a complex phenomenon.  
 117 According to Blight et al. [23], Duthinh [24] and Yang et al. [25], ASR expansion tends to reduce  
 118 shear crack openings of damaged concrete which would result in an additional aggregate interlock  
 119 contribution. On the other hand, the reduction of concrete mechanical properties reduces the bond  
 120 and bearing capacity between the aggregates and the cement paste reducing aggregate interlock  
 121 capacity. Furthermore, it has been found that ASR might potentially cause distress within the  
 122 aggregate particles, which may result in a decrease of aggregates interlock.

123 According to Sanchez et al. [6] ASR crack development in plain concrete (i.e., without reinforcing  
 124 bars) under free expansion can be described in a two-step processes: a) first, crack formation  
 125 happens within the reactive aggregate particles at low expansion levels (about 0.05% expansion)  
 126 and; b) then these cracks extend into the cement paste, establishing important crack networks as  
 127 the expansion level increases. Moreover, the authors proposed a qualitative damage model that

128 displays the crack types (Type A – sharp cracks; Type B – onion skin cracks) and their  
129 development as a function of ASR expansion for plain concrete (see Figure 3).



131 Figure 3: Qualitative ASR damage model as a function of expansion for plain concrete (adapted  
132 from Sanchez et al. [6])

## 133 2 SIGNIFICANCE OF ASR EXPANSION

134 To the authors' knowledge, no investigation has been carried out to investigate the influence of  
135 ASR on aggregate interlock with direct shear tests. A number of studies were conducted to assess  
136 the structural implications of ASR-induced expansion and damage in shear for shear critical  
137 members (Figure 1a) [26-29]. Some experimental studies showed an increase in shear capacity as  
138 a function of ASR development due to the so-called "chemical prestressing" mechanism (i.e.,  
139 expansion of concrete due to ASR induces tension in the reinforcement causing compression  
140 across the shear crack interface [29-31]). On the other hand, other experimental investigations  
141 performed on ASR affected members (e.g., bridge decks) have demonstrated that the actual  
142 capacity found was only about 75% of the expected non-damaged members [30, 31]. It is clear  
143 that there is no general agreement on the effects of ASR on the shear capacity of affected members  
144 and hence further studies are needed.

## 145 3 METHODOLOGY

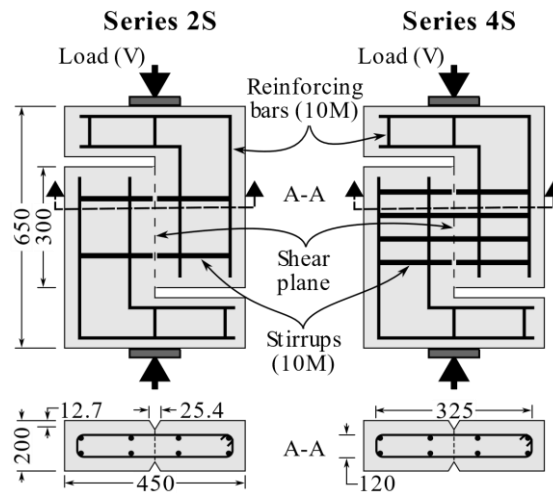
146 To investigate the effect of ASR on aggregate interlock, direct shear tests were carried out on  
147 reinforced concrete specimens containing highly reactive coarse aggregates. The responses of  
148 these specimens were studied at selected expansion levels.

### 149 3.1 Details of push-off specimens

150 Twenty-six push-off specimens were fabricated to investigate aggregate interlock in ASR affected  
151 concrete (see Figure 4 and Figure 5). Notches of 12.7 mm deep were made to ensure that the shear

152 plane was located at the center of the specimens over a height of 300 mm (see Figure 4b). The  
 153 resulting shear plane area,  $A_c$ , is equal to 52380 mm<sup>2</sup>.

154 A first series of two specimens, Series “0S”, was reinforced with 10M reinforcing bars (bar  
 155 diameter,  $d_b$ , of 11.3 mm and area,  $A_b$ , of 100 mm<sup>2</sup>) but did not contain any stirrups (specimens  
 156 not illustrated in Figure 4). These two specimens were not used for push-off tests but were used to  
 157 compare ASR-induced expansion. The other specimens were reinforced with 10M reinforcing bars  
 158 and different amounts of closed 10M stirrups across the shear plane (see Figure 4). A second series  
 159 of twelve specimens, Series “2S”, was reinforced with two 10M closed stirrups (total stirrups area,  
 160  $A_s$ , of 400 mm<sup>2</sup>), which represent a reinforcement ratio,  $\rho = A_s / A_c$ , of 0.76%. A third series of  
 161 twelve specimens, Series “4S”, was reinforced with four 10M closed stirrups ( $A_s = 800$  mm<sup>2</sup>),  
 162 which represent a reinforcement ratio of 1.53%. Specimens of the series 2S and 4S were used for  
 163 push-off testing as well as for ASR expansion monitoring.



164

165 Figure 4: Push-off specimens of Series 2S and 4S with two and four stirrups, respectively  
 166 (dimensions in mm)

### 167 3.2 Materials properties

168 Grade 400 [32] was used for the 10M reinforcing bars (Young modulus,  $E_s$ , of 200 000 MPa and  
 169 measured yield strength,  $f_y$ , of 436 MPa). A 35 MPa concrete mixture enabling a fast ASR  
 170 development in the laboratory was selected for this study. The coarse aggregates ranged from 5 to

171 20 mm in size ( $a_g = 20$  mm in Eq. (6)). Non-reactive fine aggregate was used in combination with  
 172 a highly reactive gravel from New Mexico, USA. The concrete mixture was made with a  
 173 conventional (CSA Type GU, ASTM Type I) high-alkali (0.88%  $\text{Na}_2\text{O}_{\text{eq}}$ ) Portland cement.  
 174 Reagent grade NaOH was used to raise the total alkali content of the mixtures to 1.25%  $\text{Na}_2\text{O}_{\text{eq}}$ ,  
 175 by cement mass, for accelerating the expansion process due to ASR. Table 1 gives the detailed  
 176 aggregate properties and Table 2 shows the concrete mix design.

Aggregate Identification			Rock Type Reactive rock types are in bold	Specific gravity ( $\text{g}/\text{cm}^3$ )	Absorption (%)	AMBT <sup>1</sup> 14d exp,%
Type	Reactivity	Designation (location)				
Coarse	Reactive	New Mexico (USA)	Polymictic gravel ( <b>mixed volcanic, quartzite, chert</b> )	2.53	1.59	1.114
Fine	Non-reactive	Quebec (Canada)	Natural derived from granite	2.71	0.54	0.032

177 <sup>1</sup> Accelerated Mortar bar expansion at 14 days [33].

178 Table 1: Aggregates properties

Concrete Mix design	Ingredients	Materials ( $\text{kg}/\text{m}^3$ )	Materials ( $\text{L}/\text{m}^3$ )
		Mixtures NM gravel	Mixtures NM gravel
Components	Cement	370	118
	Sand	714	264
	Coarse aggregate	1073	424
	Water	174	174
	Air	-	20.0
	Alkalis	4.63	-
	w/c	0.47	-

179 Table 2: Concrete mix proportions.



180 3.3 Concrete curing and ASR expansion measurement

181 The specimens were placed in the moist curing room immediately after casting for a 7-day curing  
182 period, after which they were demolded. Holes, 10 mm in diameter by 65 mm long, were drilled  
183 into each specimen (Figure 5a) and stainless steel gauge studs were installed, with fast-setting  
184 cement slurry, to measure the expansion perpendicular to the shear plane.

a)



b)



c)



185 Figure 5: (a) Push-off specimen used and stud locations for ASR expansion measurement, (b)  
186 storage of specimens in sealed plastic containers and (c) ASR measurement

187 The specimens were then stored in the laboratory for 48h at 23°C, after which the “0” length  
188 reading was performed and the specimens were placed in sealed plastic containers lined with  
189 dampened burlap (2 specimens per container, Figure 5b). All containers were stored at 38°C and  
190 100% R.H., and all the push-off specimens were monitored regularly for length variations (see  
191 Figure 5c). As per ASTM-C1293 [34], the containers were cooled to 23 °C for  $16 \pm 4$  h prior to  
192 periodic expansion measurements.

193 To estimate the targeted ASR expansion for push-off specimens, the concrete expansion was  
194 monitored in the two specimens without stirrups (Series 0S). Then, expansion levels of  $0.05\% \pm$   
195  $0.01$  and  $0.12\% \pm 0.01\%$  were selected for half of the push-off specimens of the series 2S and 4S.  
196 The push-off specimens reaching an expansion of  $0.05\%$  and  $0.12\%$  were designated as “R5” and  
197 “R12”, respectively. These expansion levels were chosen according to desired ASR damage levels  
198 observed microscopically by Sanchez et al. [6]. Once these expansion levels were reached after a  
199 conditioning period of time, specimens were wrapped in plastic film and stored at  $12^{\circ}\text{C}$  to limit  
200 ASR progression until testing as described by Sanchez et al. [6].

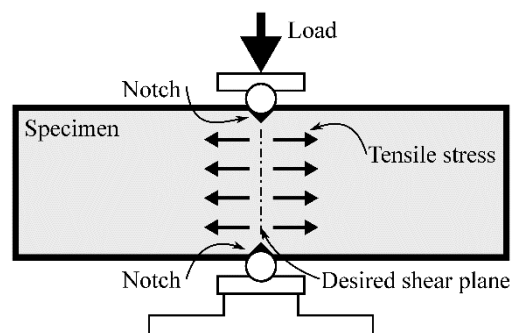
201 For comparison, non-reactive concrete specimens designated as “NR5” and “NR12” were tested.  
202 These specimens were fabricated with the same mix-design and stored in similar conditions and  
203 the same conditioning period as the corresponding specimens R5 and R12, but lithium-based  
204 admixtures were used in the concrete mix to inhibit ASR development.

#### 205 3.4 Loading procedure and measurements of push-off specimens

206 Prior to testing, the specimens were kept for 48h in the moist curing room to allow appropriate re-  
207 saturation [35]. Then the push-off test was carried out in the following two steps.

##### 208 3.4.1 *Pre-cracking phase*

209 All the specimens were pre-cracked along the critical shear plane before push-off testing. Steel  
210 plates designed to fit the shear plane notches were placed under and over the notches and then  
211 loaded at a rate of  $0.3 \text{ mm/min}$  to create tensile stresses and cracking along the desired shear plane  
212 (see Figure 6). The pre-cracking phase was completed when the crack width measured by four  
213 linear variable differential transformers (LVDT) (two on each side of the critical shear section, see  
214 Figure 7a) reached a crack width of  $0.10 \text{ mm}$ .



215

216

Figure 6: Pre-cracking of a push-off specimen

a)



b)



217 Figure 7: (a) Measurements of crack width during pre-cracking phase by four LVDTs (two on  
218 each side) and (b) crack width and slip during push-off testing

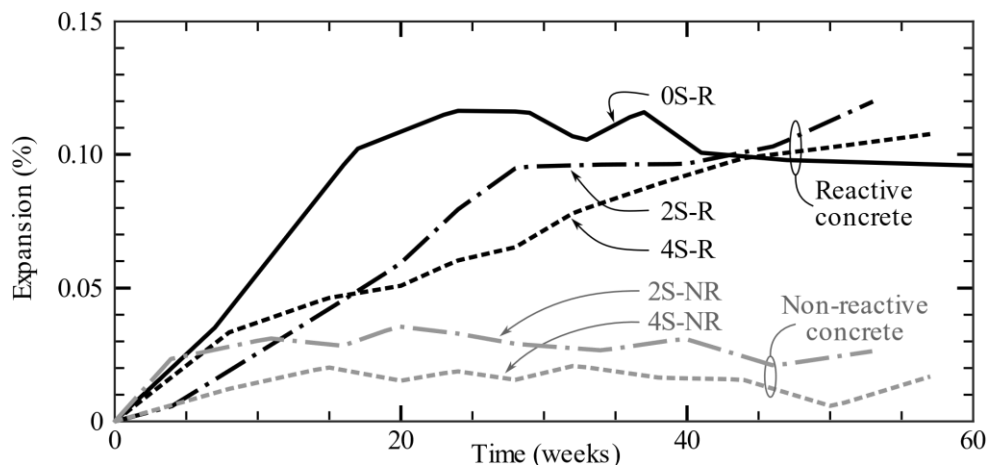
### 219 3.4.2 Push-off testing

220 The four LVDTs used during pre-cracking remained on the specimen to measure crack width  
221 during push-off testing. In addition, two new LVDTs (1 per side, see Figure 7b) were installed to  
222 measure crack slip. The specimen was placed in the testing frame as illustrated in Figure 7b and  
223 then loading was applied at a rate of 0.25 mm/min. The test was considered completed when the  
224 average crack slip reached approximately 2 mm, which is considered to be large enough to  
225 evaluate the aggregate interlock shear behavior [34].

## 226 4 ASR DEVELOPMENT ON THE CONCRETE SPECIMENS

227 Figure 8 presents representative values of expansion measured perpendicular to the shear plane  
228 (see Figure 5c). All the non-reactive concrete specimens 2S-NR and 4S-NR, due to the inclusion  
229 of lithium to control ASR expansion, showed very small expansion levels over time (i.e. generally

230 lower than 0.03%). The specimens with reactive concrete, 0S-R, 2S-R and 4S-R (without lithium),  
 231 exhibited significant expansion. The reactive concrete specimen without reinforcement, 0S-R,  
 232 reached 0.05% and 0.10% expansion at 9 and 16 weeks (64 days and 115 days), respectively. After  
 233 24 weeks (168 days), expansion reached a maximum value of 0.12%. A longer delay was observed  
 234 for reactive concrete specimen with stirrups. The reactive concrete specimen with two stirrups, 2S-  
 235 R, reached 0.05% and 0.10% expansion at 17 and 29 weeks (121 and 203 days), respectively. The  
 236 reactive concrete specimen with four stirrups, 4S, reached 0.05% and 0.10% expansion at 19 and  
 237 45 weeks (133 and 321 days), respectively. After reaching 0.10% expansion, the rate of expansion  
 238 slowed down and maximum values of 0.12% and 0.11% were reached after 53 and 57 weeks (371  
 239 and 399 days) for the representative specimens 2S-R and 4S-R presented in Figure 8, respectively.  
 240 It is clear that increased confinement due to increasing the amount of stirrups delayed the measured  
 241 expansion.



242  
 243 Figure 8: Typical values of ASR expansion as a function of time for reactive and non-reactive  
 244 concrete specimens with different amounts of stirrups

245 5 PUSH-OFF TESTS RESULTS AND DISCUSSION

246 5.1 Test results

247 Figure 9 and Table 3 present the push-off test results for the reactive and non-reactive concrete  
 248 specimens. Figure 9 shows the aggregate interlock shear stress,  $v_{ci}$ , the average shear stress due to  
 249 dowel action of the stirrups,  $\rho v_d$ , the crack width,  $w$ , and the compressive stress on the crack  
 250 interface,  $f_{ci}$ , as a function of the crack slip,  $\delta$ . These average values for each series were

251 determined for each value of slip. Table 3 compares the average peak values of aggregate interlock,  
 252  $v_{ci,peak}$ , and the corresponding compressive stress on crack interface,  $f_{ci,peak}$ , crack slip,  $\delta_{peak}$ , and  
 253 width,  $w_{peak}$ , for all the reactive and non-reactive concrete specimens. This table also presents the  
 254 measured expansion levels at the time of testing each specimen.

255 The aggregate interlock shear stress was determined with Eq. (1) by taking the total shear stress,  
 256  $V/A_c$ , and subtracting the shear stress due to dowel action of the stirrups,  $\rho v_d$ . The model  
 257 proposed by Maekawa et al. [36] and Moradi et al. [37] was used to determine  $v_d$ . This model  
 258 validated by several authors [37-41] considers interaction between the shear stress and the axial  
 259 stress in the stirrups at a crack and can be expressed as:

$$260 \quad v_d = \frac{12.1 f_c'^{0.6375} E_s^{0.25}}{d_b k_{di}^3} \delta \leq \frac{f_y}{\sqrt{3}} \sqrt{1 - \left( \frac{f_s}{f_y} \right)^4} \quad (7)$$

261 In this equation,  $f_s$  is the axial stress in the stirrups at a crack and  $k_{di}$  is a concrete damage  
 262 parameter that considers the bar diameter, the crack width and slip. Considering an initial stirrup  
 263 deformation caused by ASR,  $\varepsilon_{s0}$ , and an elastic strain-hardening stress-strain response, the stirrups  
 264 axial stress,  $f_s$ , is determined from the crack opening as follows [42-44]:

$$265 \quad f_s = \sqrt{\frac{2E_s f_c'^{2/3}}{d_b} w} + E_s \varepsilon \quad w \leq w_y \quad (8)$$

$$266 \quad f_s = \sqrt{\frac{2E_h f_c'^{2/3}}{d_b} (w - w_y)} + E_h \varepsilon_{s0} + f_{yr} \quad w > w_y \quad (9)$$

267 Where  $E_h$  is the strain-hardening modulus (taken as 1000 MPa),  $f_{yr}$  is a reduced yield strength  
 268 that considers the effect of shear stress from Eq. (10) [36] and  $w_y$  is the crack width at the yielding  
 269 of the stirrups given by Eq. (11).

$$270 \quad f_{yr} = f_y \sqrt[4]{1 - 3(v_d / f_y)^2} \quad (10)$$

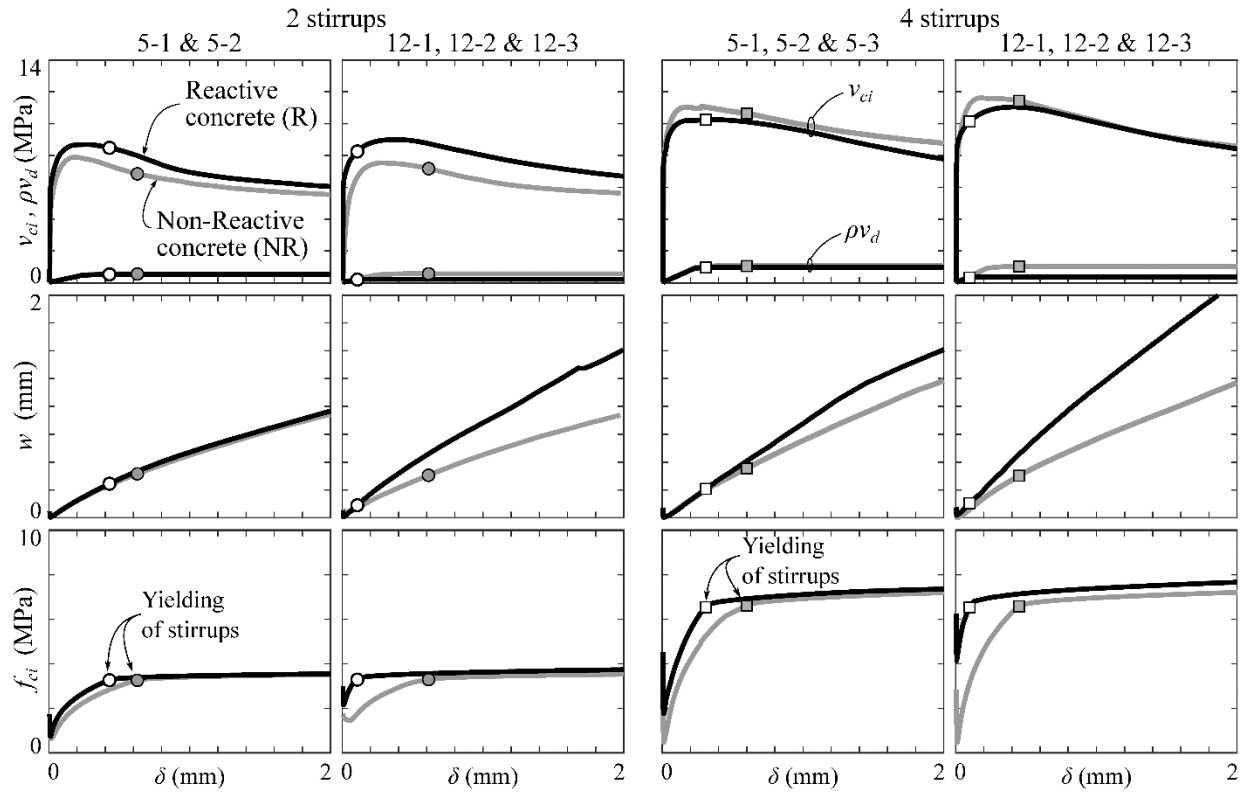
$$271 \quad w_y = \frac{d_b E_s}{2 f_c'^{2/3}} \left( \frac{f_{yr}}{E_s} - \varepsilon_{s0} \right)^2 \quad (11)$$

272 The ASR-induced expansion of the specimens was measured 65 mm from the specimen surface  
 273 and the initial stirrups strain,  $\varepsilon_{s0}$ , was taken equal to the concrete expansion at this location.

		Reactive concrete (R)							Non reactive concrete (NR)						R/NR	
Test*	cure weeks	$\varepsilon_{ASR}$	$f'_c$	$\delta_{peak}$	$w_{peak}$	$v_{ci,peak}$	$f_{ci,peak}$	$\varepsilon_{ASR}$	$f'_c$	$\delta_{peak}$	$w_{peak}$	$v_{ci,peak}$	$f_{ci,peak}$	$\frac{v_{ci,peakR}}{v_{ci,peakNR}}$	$\frac{f_{ci,peakR}}{f_{ci,peakNR}}$	
		%	MPa	mm	mm	MPa	MPa	%	MPa	mm	mm	MPa	MPa			
2S	5-1	39.9	0.029	42.6	0.20	0.17	8.87	2.46	0.009	45.0	0.22	0.14	8.32	1.99	1.07	1.23
	5-2	17.9	0.050	41.6	0.30	0.21	8.49	3.00	0.013	43.7	0.16	0.15	7.49	2.10	1.13	1.43
	12-1	46.1	0.088	42.7	0.24	0.29	9.58	3.45	0.018	45.1	0.26	0.15	6.92	2.20	1.38	1.57
	12-2	53.1	0.120	42.8	0.40	0.36	8.88	3.51	0.022	45.2	0.38	0.28	7.82	2.98	1.14	1.18
	12-3	53.1	0.139	42.8	0.45	0.47	8.62	3.56	0.027	45.2	0.28	0.24	7.90	2.85	1.09	1.25
	Average			42.5	0.32	0.30	8.89	3.20		44.8	0.26	0.19	7.69	2.42	1.16	1.33
4S	5-1	28.0	0.049	45.2	0.18	0.13	9.81	5.12	0.013	47.1	0.26	0.23	11.74	5.31	0.84	0.96
	5-2	59.0	0.049	42.9	0.17	0.14	10.59	5.17	0.000	46.9	0.15	0.11	10.62	3.42	1.00	1.51
	5-3	23.9	0.059	45.0	0.51	0.47	10.52	6.92	0.008	46.9	0.17	0.12	10.77	3.75	0.98	1.85
	12-1	50.1	0.098	45.7	0.45	0.53	10.77	7.10	0.004	47.6	0.15	0.13	11.76	3.83	0.92	1.85
	12-2	57.1	0.108	45.8	0.29	0.46	12.12	7.09	0.017	47.7	0.26	0.21	12.13	5.20	1.00	1.36
	12-3	66.0	0.115	43.0	0.48	0.59	10.35	7.15	0.017	47.0	0.18	0.16	10.97	4.64	0.94	1.54
Average			44.4	0.38	0.44	10.87	6.69		47.2	0.18	0.15	11.25	4.17	0.94	1.51	

274 \* No result was monitor for the specimens 2S-5R-3 and 2S-5NR-3 due to the measuring system malfunction

275 Table 3: Summary of push-off test results for specimens with two and four stirrups



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Figure 9: Average values of: shear stress at crack due to aggregate interlock,  $v_{ci}$ , dowel resistance,  $\rho v_d$ , crack width,  $w$ , and the compressive stress on crack,  $f_{ci}$ , as a function of the crack slip,  $\delta$

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## 5.2 Influence ASR-induced expansion level and amount of stirrups

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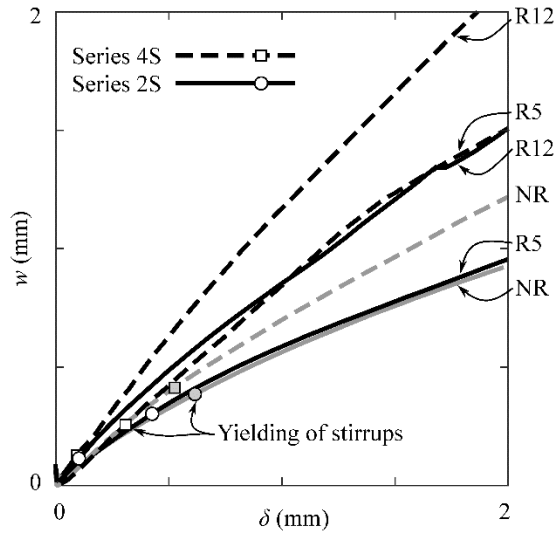
It can be seen from Figure 9 that, before any shear was applied, the specimens exhibit a very small crack (less than 0.1 mm) due to precracking. This precracking caused tensile stress in the stirrups and an initial compressive stress on the crack interface,  $f_{ci}$ . ASR expansion levels induces additional tensile stresses in the stirrups (i.e. “chemical” prestressing) and increased compressive stresses on the crack interface. As the amount of stirrups and ASR expansion increase, this initial compressive stress on the crack interface applied by the stirrups increases. For example, the compressive stress on the crack due to chemical prestressing of the stirrups in the reactive concrete specimens with two stirrups, R5 and R12, reaches on an average 0.65 and 1.76 MPa, which represents 20% and 53% of the stirrup yield stress, respectively.

290 When shear is applied, the compressive stress on the crack interface applied by the stirrups tends  
291 to close the shear crack. For the same applied shear, the initial stress due to ASR chemical  
292 prestressing results in a smaller shear crack width than the specimens with non-reactive concrete.  
293 As the initial compressive stress on the crack interface increases, friction on the crack interface  
294 increases and a larger shear stress must be applied to start the shear crack opening and sliding.  
295 Thus, the initial slope of the shear stress versus slip curve in Figure 9 is steeper for the reactive  
296 specimens (R5 and R12) than the non-reactive ones (NR5 and NR12).

297 When crack slip occurs, the shear stress due to dowel action of the stirrups is engaged. However,  
298 it can be seen in Figure 9 that the shear stress carried by the stirrups,  $\rho v_d$ , is relatively small  
299 compared to the aggregate interlock,  $v_{ci}$ . For Series 2S and 4S, the shear stress due to dowel action,  
300  $\rho v_d$ , reached an average 0.37 MPa and 0.62 MPa, respectively (see Figure 9) at the peak aggregate  
301 interlock shear stress. The shear stress due to dowel action represents less than 6% of  $v_{ci,peak}$ . At  
302 the end of the test,  $v_{ci}$  decreases and  $\rho v_d$  represents less than 11% of  $v_{ci}$ .

303 When the applied shear increases, the aggregate interlock becomes fully engaged and the crack  
304 slips and opens. The relationship between the average crack width and the average crack slip is  
305 shown in Figure 10 for the push-off specimens. It can be seen in Figure 9 and Figure 10 that this  
306 crack displacement is similar for reactive and non-reactive concrete specimens up to the yielding  
307 of the stirrups. Yielding of the stirrups occurs at similar crack displacements for the specimens  
308 with two and four stirrups. However, increasing ASR reduces the crack width at stirrup yielding  
309 since the stirrups were in tension before shear was applied. On average, crack widths of 0.60 mm,  
310 0.40 mm and 0.15 mm and crack slips of 0.30 mm, 0.25 mm and 0.10 mm were determined when  
311 the stirrups yielded for the specimens NR, R5 and R12, respectively.





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Figure 10: Average crack width,  $w$ , versus average crack slip,  $\delta$

314 After the stirrups reach yielding, the increase of crack width does not result in a significant  
 315 increases of compressive stress at the crack interface,  $f_{ci}$ , and the crack opens (see Figure 9).

316 Because the yielding of the stirrups occurs at smaller slips for the reactive concrete specimens, the  
 317 crack width becomes larger for these specimens than for the non-reactive concrete specimen after  
 318 stirrups yielding (see Figure 9 and Figure 10). Consequently, the peak-aggregate interlock  
 319 generally occurs after yielding of the stirrups for the specimens with more significant ASR  
 320 expansion. At the peak aggregate interlock, the specimens R12 with two and four stirrups reached  
 321 on an average  $f_{ci,peak}$  of 3.51 MPa and 7.11 MPa, respectively (see Table 3), which exceed the  
 322 stirrups yielding. For the non-reactive specimens with two and four stirrups, stirrups are elastic  
 323 and the compressive stress at the crack interface was on average 2.42 MPa and 4.17 MPa,  
 324 respectively. This compressive stress slightly increases to 2.73 MPa and 5.74 MPa for the  
 325 specimens R5 with two and four stirrups, respectively.

326 For the non-reactive concrete specimens with two stirrups, the average peak aggregate interlock  
 327 stresses,  $v_{ci,peak}$ , reached 7.69 MPa compared to 11.25 MPa for the specimens with four stirrup.

328 That increase of aggregate interlock can be attributed to the larger compressive stress on the crack  
 329 interface for the specimen with four stirrups. The non-reactive concrete specimens with two and  
 330 four stirrups exhibited similar crack widths at the peak but the specimens with four stirrups  
 331 experienced a compressive stress on the crack interface about twice as much as the specimens with

332 two stirrups. These results show that increasing the amount of stirrups increases  $f_{ci,peak}$ , and hence  
333  $v_{ci,peak}$ .

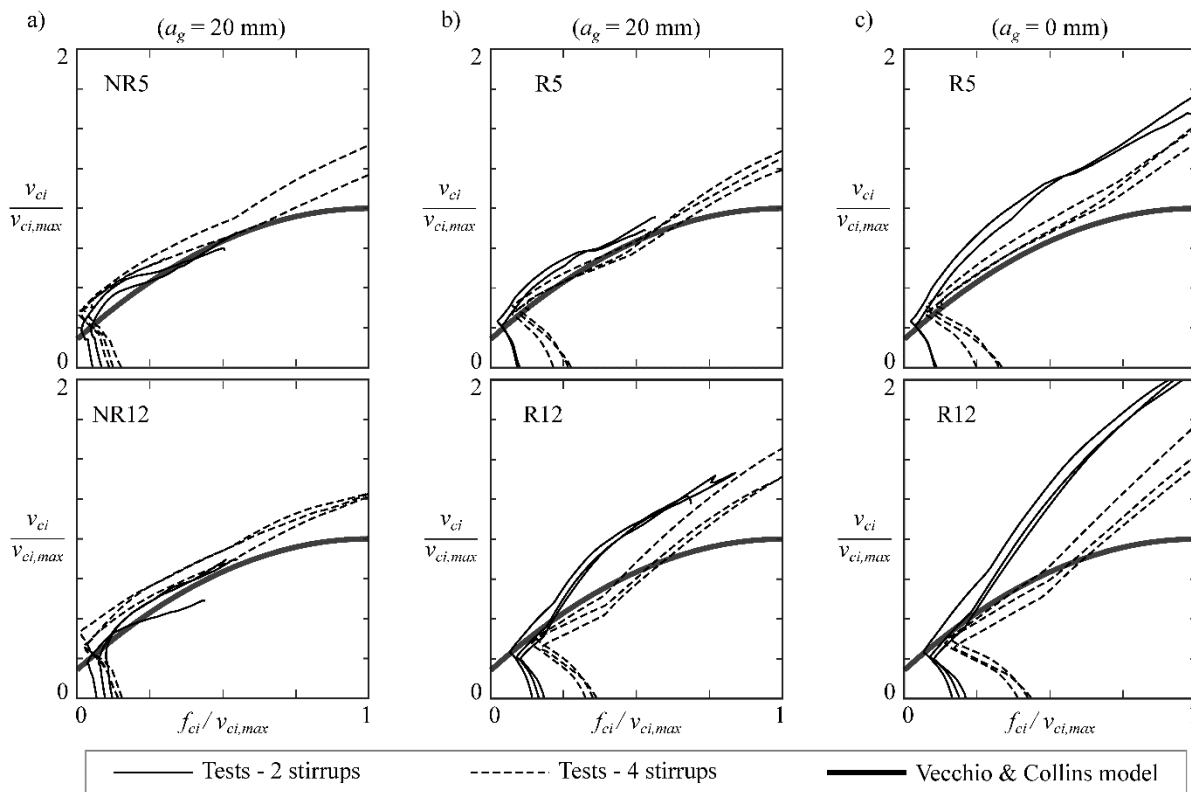
334 Increasing ASR expansion also increases  $f_{ci,peak}$  and hence  $v_{ci,peak}$ . However, yielding of the  
335 stirrups also occurs sooner for the reactive concrete specimens and the resulting larger crack tends  
336 to reduce  $v_{ci,peak}$ . These two opposite effects were observed by comparing the specimens with two  
337 and four stirrups. For the specimens with two stirrups, increases of  $w_{peak}$  of 58% (from 0.19 mm  
338 to 0.30 mm, see Table 3) and  $f_{ci,peak}$  of 33% were determined for the reactive concrete specimens  
339 compared to the non-reactive concrete specimens. This increase results in a peak aggregate  
340 interlock increase of 16% on average (from 7.69 MPa to 8.89 MPa) for the reactive concrete  
341 specimens compared to the non-reactive concrete specimens. On the contrary, for the reactive  
342 concrete specimens with four stirrups (Series 4S), the peak aggregate interlock decreased by 6%  
343 on average compared to the non-reactive concrete specimens (from 11.25 MPa to 10.87 MPa). For  
344 these reactive concrete specimens with four stirrups, the crack width at the peak increased by 162%  
345 (0.15 mm compared to 0.44 mm) while the compressive stress on the crack interface increased by  
346 51% compared to the non-reactive concrete specimens.

347 Accounting for the microscopic model displayed in Figure 3, expansion increases ASR damage in  
348 concrete, which may result in reductions in both mechanical properties and aggregate interlock.  
349 The push-off specimens with four stirrups presented higher shear capacities than the specimens  
350 with two stirrups. However, for the case of significant ASR-induced expansion, increasing the  
351 amount of stirrups results in higher localized stresses on the shear crack interface which tends to  
352 give rise to greater strength reductions than the specimens that are not affected by ASR.

## 353 6 COMPARISON OF PREDICTIONS WITH PUSH-OFF TEST RESULTS

354 The aggregate interlock model proposed by Vecchio et al. [18] (Eq. (5)) considers the concrete  
355 strength, aggregate size and the crack opening to define the maximum aggregate interlock,  $v_{ci,max}$   
356, that can be transmitted across a crack when sufficient stirrups are provided. Increasing the crack  
357 width and reducing the aggregate size results in lower values of  $v_{ci,max}$ . The aggregate interlock  
358 shear stress is then determined from the compressive stress on the crack interface,  $f_{ci}$ , and the

359 maximum aggregate interlock,  $v_{ci,max}$ . When the shear crack runs through the aggregate particles,  
 360 the aggregate interlock mechanism illustrated in Figure 2 is no longer valid, which may  
 361 significantly reduce the maximum aggregate interlock,  $v_{ci,max}$ . In this case, Angelakos et al. [19]  
 362 suggested using a reduced aggregate size of  $a_g = 0$  to determine the maximum aggregate interlock,  
 363  $v_{ci,max}$ . High levels of ASR can result in a similar crack pattern through the aggregate particles (see  
 364 Figure 3) and a reduced aggregate interlock shear stress. Figure 11 compares the predictions using  
 365 the Vecchio and Collins model with the push-off test results. For these predictions, the real  
 366 aggregate size ( $a_g = 20$  mm) and a reduced one for cracks running through the aggregate particles  
 367 ( $a_g = 0$  mm) were considered to determine  $v_{ci,max}$ .



368  
 369 Figure 11: Comparison of predictions using Vecchio et al. [18] model with test results for (a)  
 370 non-reactive concrete specimens ( $a_g = 20$  mm), (b) reactive concrete specimens considering  
 371 sound aggregates ( $a_g = 20$  mm) and (c) fractured aggregates ( $a_g = 0$ )

372 The push-off test specimens before any shear is applied have an initial compressive stress across  
373 the crack interface,  $f_{ci}$ , due to the presence of ASR and the initial cracking along the shear  
374 interface (see Figure 11). As shear is applied to a specimen, the crack width and  $f_{ci}$  initially  
375 decreases as the interlock along the interface starts to be engaged. When the aggregate interlock is  
376 engaged, the shear stress ratio reaches the Vecchio et al. [18] model curve, which corresponds to  
377  $v_{ci} / v_{ci,max}$  of about 0.18 for the non-reactive concrete specimens. Then, the crack opens and the  
378 compressive stress across the crack increases. Increasing the initial prestressing caused by ASR  
379 increases the initial ratio  $f_{ci} / v_{ci,max}$  so that the crack opening and slippage begin at a shear stress  
380 ratio  $v_{ci} / v_{ci,max}$  larger than 0.18. The opening of the crack reduces  $v_{ci,max}$  and the ratios  $v_{ci} / v_{ci,max}$   
381 and  $f_{ci} / v_{ci,max}$  increase, even after yielding of the stirrups and after reaching the peak aggregate  
382 interlock,  $v_{ci,peak}$  (see Figure 9 and Figure 11).

383 By considering the sound maximum aggregate size ( $a_g = 20$  mm) to determine  $v_{ci,max}$ , it appears  
384 that the Vecchio & Collins model provides a good estimation of the aggregate interlock shear  
385 behavior and capacity (see Figure 11). In order to compare the model predictions with the test  
386 values for each specimen, the peak value of  $v_{ci}$  obtained from the test and the corresponding  $w$   
387 and  $f_{ci}$  were used in Eq. (5) and (6) to determine the corresponding model peak value. For non-  
388 reactive concrete specimens, with 2 stirrups and 4 stirrups, NR5 and NR12, the peak aggregate  
389 interlock is slightly underestimated by the model (average model/test value of 0.82, coefficient of  
390 variation, CoV, of 6.8%). Very similar peak aggregate interlock underestimation is provided by  
391 the model for reactive concrete specimens R5 and R12 when sound aggregates are considered  
392 (average model/test value of 0.85, CoV of 10.8%).

393 By considering fractured aggregates ( $a_g = 0$ ) to determine  $v_{ci,max}$  for reactive concrete specimens,  
394 it can be seen from Figure 11c that the predictions using the Vecchio & Collins model gives an  
395 overly conservative estimate of the aggregate interlock. On average for reactive concrete  
396 specimens R5 and R12, the peak shear stress,  $v_{ci,peak}$ , determined from the test is 33% larger than  
397 the model predictions (average model/test value of 0.67). Furthermore,  $v_{ci,peak}$ , is underestimated  
398 by the model for all the tests and the scattering between experimental tests and Eq. (5) is even

399 larger for the ASR reactive concrete specimens than for the non-reactive concrete specimens (CoV  
400 = 19% for reactive concrete specimens). Hence, it can be concluded that considering fractured  
401 aggregates ( $a_g = 0$ ) in Eq. (5) and (6) is not appropriate for the specimens subjected to ASR  
402 expansion levels in this study.

## 403 7 CONCLUSIONS:

404 The main objective of this research was to better understand the influence of ASR on aggregate  
405 interlock of reinforced concrete specimens. The main findings are presented here after:

- 406 • Confinement due to increased amounts of stirrups delayed the ASR-induced expansion in the  
407 direction parallel to the stirrups. However, the confinement did not affect the maximum  
408 expansion level reached by the specimens.
- 409 • Increasing ASR-induced expansion and the amount of stirrups increases the initial tensile stress  
410 in the stirrups and the compressive stress transmitted across the shear crack interface.  
411 Consequently, a larger shear must be applied to initiate crack opening and slippage and the  
412 stirrups across the shear crack yield at a smaller slip for the ASR-affected concrete specimens.
- 413 • After stirrup yielding, the reactive concrete specimens experience larger shear cracks than the  
414 non-reactive concrete specimens.
- 415 • No significant reduction in aggregate interlock was attributed to ASR-induced damage for the  
416 tested specimens subjected to ASR having expansion levels less than about 0.12%.
- 417 • There are two opposing effects for ASR-affected concrete: a larger compressive stress across  
418 the crack interface increases aggregate interlock while a larger shear crack width reduces  
419 aggregate interlock. ASR-affected concrete specimens experience these two opposite effects  
420 and aggregate interlock may increase or decrease regarding their relative importance.
- 421 • The Vecchio and Collins aggregate interlock model considers these two effects. For the ASR  
422 expansion levels studied, this model predicts well the aggregate interlock shear behavior when  
423 the real aggregate size is considered. It therefore appears that the potential cracking through  
424 the aggregate particles did not progress enough to reduce aggregate resistance and interlock.

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